Grange Primary School

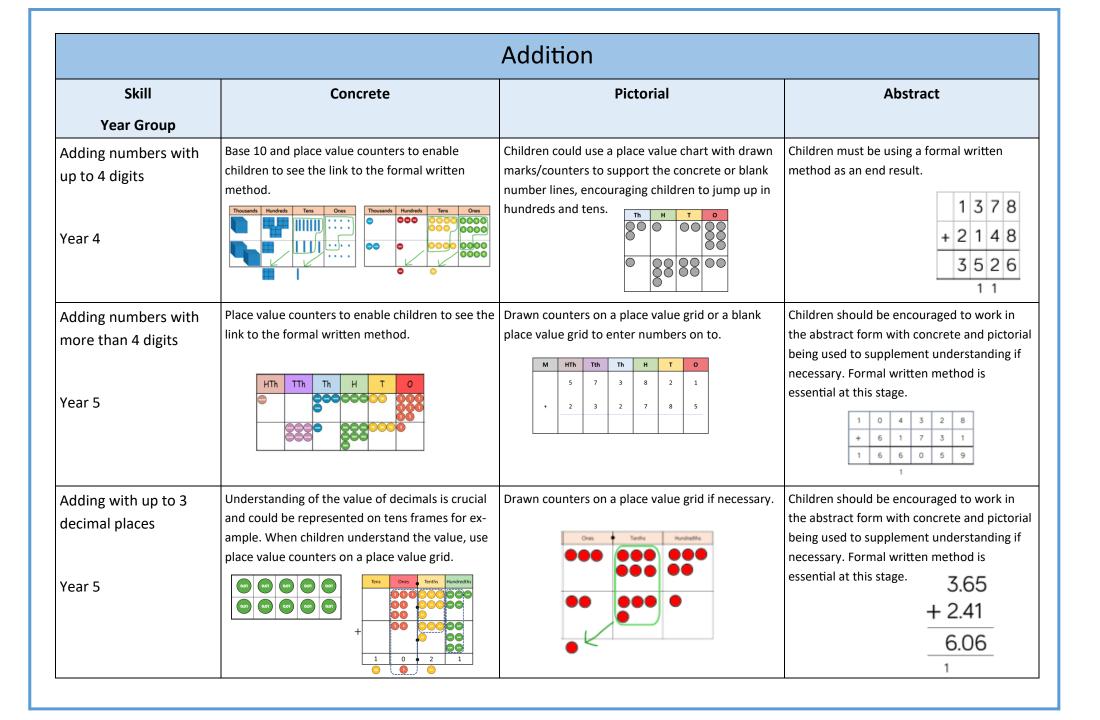


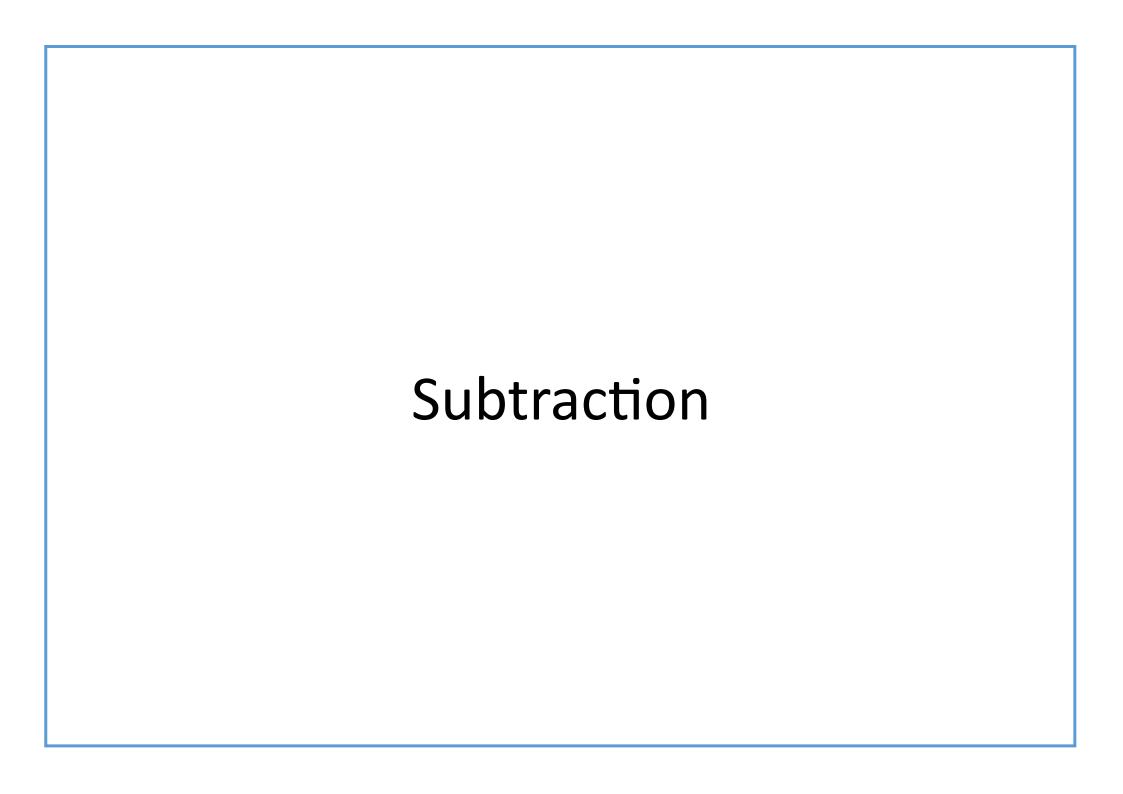
Calculation Policy

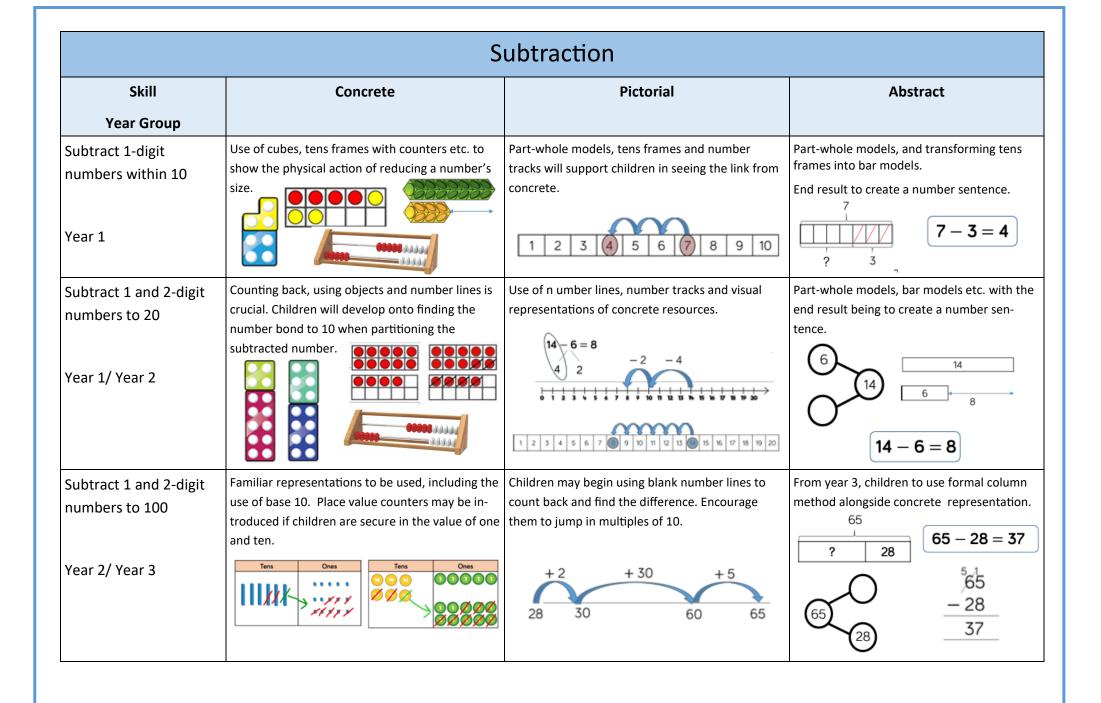


		Addition	
Skill Year Group	Concrete	Pictorial	Abstract
Adding 1-digit numbers within 10 Year 1	Use people or objects to show combining two separate 1-digit numbers into a new total.	Move to part-whole models or tens frames using the same representative as the concrete lesson. Children to move onto drawing to represent the calculation. Use of number tracks for counting on.	Progress to using numerals in the part whole models and transforming the tens frames into bar models. End result will be writing a number sentence. $ 7 $ $ 4 + 3 = 7 $
Adding 1 and 2-digit numbers to 20 Year 1 / Year 2	When adding digits that cross 10, it is important children understand the importance of ten ones equalling one ten.	Move to using familiar models such as part-whole models and number tracks. Year 2 may progress to number lines (alongside the concrete resources) to support the children in understanding how to partition their jumps. 8 + 7 = 15 1 2 3 4 5 6 7 8 9 10 11 12 13 14 8 16 17 18 19 20 + 2 + 5	Progress to using numerals in the part whole models and transforming the tens frames into bar models. End result will be writing a number sentence. $ \begin{array}{c c} & 15 \\ \hline & 8 \\ \hline & 7 \\ \hline & 8 \\ \hline & 8 \\ & 7 $
Adding three 1-digit numbers	Children should be encouraged to look for number bonds to 10 (with manipulatives highlighting this) or doubles .This develops understanding of commutativity.	Progress to familiar models such as part-whole models. Number lines could be used to help reinforce the bonds to 10.	Progress to using numerals in the part whole models and transforming the tens frames into bar models. End result will be writing a number sentence.
Year 2			7 + 6 + 3 = 16 7 6 3

		Addition	
Skill Year Group	Concrete	Pictorial	Abstract
Adding 1-digit and 2-digit numbers to 100 Year 2	Children should be encouraged to count on from the larger number. Begin with familiar manipulatives that have been used so far and progress onto base 10. Large number squares and number lines may be useful. 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 56 17 18 19 12 12 12 12 12 12 12 12 12 12 12 12 12	Use of number lines, number tracks, hundred squares etc. could help to show bonds to 10.	Progress to using numerals in the part whole models and transforming the tens frames into bar models. End result will be writing a number sentence $\frac{38}{38}$ $\frac{38}{38}$ $\frac{38}{38}$ $\frac{38}{38}$ $\frac{38}{38}$
Adding two 2-digit numbers to 100 Year 2 / Year 3	Use of base 10 to begin to show the exchange of ones cubes to a tens stick. Familiar representatives could also be used if appropriate. Place value counters may be introduced if children are secure in the value of one and ten.	Blank number lines to allow counting on are essential with children encouraged to jump up in tens to become more efficient. + 2 + 21 38 40 61	End result will be writing a number sentence to represent the concrete/pictorial method. Year 3 will use the formal written method when calculating alongside the base 10 and place value counter representations. $ 38 \\ + 23 \\ \hline 61 \\ 1 $ $ 38 + 23 = 61$
Adding numbers with up to 3 digits Year 3	Use of base 10 and moving onto place value counters when children are secure in understanding the value of the counters. Mundreds Tens Ones 265 164 429 1 1 1 1 1 1 1 1 1	Children could use a place value chart with drawn marks/counters to support the concrete or blank number lines, encouraging children to jump up in hundreds and tens.	Children should be beginning to represent their calculation as a formal written method for addition. 265 + 164 429







	S	ubtraction	
Skill Year Group	Concrete	Pictorial	Abstract
Subtract numbers with up to 3 digits Year 3	Base 10 and place value counters are the most effective manipulative to use when subtracting 3 digits. Ensure children understand the value of 1,10,100 etc before using.	Children could use a place value chart with drawn marks/counters to support the concrete or blank number lines, encouraging children to jump up in hundreds and tens.	Written column method to be used alongside the concrete resources so that the link can be easily seen. 3435 273 162
Subtract numbers with up to 4 digits Year 4	Base 10 and place value counters are to be used at this stage. Thousands Hundreds Tens Ones Thousands Hundreds Tens Ones Thousands Hundreds Tens Ones	Place value charts with drawn marks/counters could be used to support. Th H T O O O O O O O O O O O O O O O O O O	Written column method to be used alongside the concrete resources so that the link can be easily seen.
Subtract numbers with more than 4 digits Year 5	Place value counters (or plain counters on a place value grid) are crucial at this stage.	Drawn counters on a place value grid or a blank place value grid to enter numbers on to. M HTh Tth H T O 2 9 4 3 8 2	Children should be encouraged to work in the abstract form with concrete and pictorial being used to supplement understanding if necessary. Formal written method is essential at this stage.
		1 8 2 5 0 1	- 1 8 2 5 0 1 1 1 1 8 8 1

	Subtraction				
Skill Year Group	Concrete	Pictorial	Abstract		
Subtract with up to 3 decimal places Year 5	Understanding of the value of decimals is crucial and could be represented on tens frames for example. When children understand the value, use place value counters on a place value grid.	Drawn counters on a place value grid if necessary.	Children should be encouraged to work in the abstract form with concrete and pictorial being used to supplement understanding if necessary. Formal written method is essential at this stage. 5.43 -2.7 -2.7		



	M	ultiplication					
Skill Year Group	Concrete	Pictorial		Ab	stract	t	
Solve 1-step problems using multiplication	Children to use concrete resources to represent problems in many different ways.	Pictorial representations to be used to represent the problems.	In year 1, the cation to be multiplication 5	recorded	I forma	ally. In	year 2, thoduced.
Year 1/2		0 1 2 5 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20		4 × 5 5 × 4			
Multiply 2-digit by 1- digit numbers Year 3/4	Place value counters and base 10 to be used to support the understanding of the method.	Pictorial representations of concrete resources could be used to as a stepping stone between concrete and abstract, but is not necessary.	Informal me used in year introduced t	3. Short o year 4.	multip	H T 3	o
Multiply 3-digit numbers by 1-digit numbers	Base 10 and place value counters can be used to support the understanding of the written method. Limit the number of exchanged needed in the questions and move children away from re-	Pictorial representations of concrete resources could be used to as a stepping stone between concrete and abstract, but is not necessary.	When movir mal written			_	short, for
Year 3/4	sources when using larger numbers.			2	4	5	
			×			4	
	20000			9	2	0	

	M	ultiplication	
Skill Year Group	Concrete	Pictorial	Abstract
Multiply 4-digit numbers by 1-digit numbers Year 5	The best concrete resources to use at this stages are place value counters. These can be used to support the understanding of the formal written method.	Pictorial representations of concrete resources could be used to as a stepping stone between concrete and abstract, but is not necessary.	Formal written method to be used with mutiplication grids used as a support for times tables id the children are struggling so that they can really focus on the method. The H T O The H T O 1 8 2 6 X 3 3 5 4 7 8 2 1
Multiply 2-digit by 2- digit numbers	Area models should be used initially to help the children understand the size of numbers they are using. Begin with Base 10 (as this leads nicely to finding the area of rectangle) and then move	Pictorial representations of concrete resources could be used to as a stepping stone between concrete and abstract, but is not necessary.	The grid method shows clearly the link between the area models and the multiplication. Children should move onto the forma written method.
Year 5	onto place value counters.		X 20 2 30 600 60 1 20 2 6 6 0 6 8 2
Multiply 3-digit numbers by 2-digit numbers Year 5	Children can continue to use area models with place value counters being the most efficient at this stage.	Pictorial representations of concrete resources could be used to as a stepping stone between concrete and abstract, but is not necessary.	Links to the grid method can be used with children moving onto the formal written method. X 200 30 4 2 3 4

Multiplication							
Skill Year Group	Concrete	Pictorial		Ab	stra	ct	
Multiply 4-digit numbers by 2-digit numbers	Area models could be used if children are still struggling to understand the mechanics of the calculation but at this stage children should be confident enough to move straight to formal written method.		this stage. Chil cation grid to h this is somethi	Formal written method should be used a this stage. Children may be given a mult cation grid to help with their times table this is something they would benefit fro Consider where digits are placed and materials.			
Year 5/6			T			Т	0
				2	7	3	9
			>			2	8
			2	1 5	9	1	2
			. ŧ	4	7	8	0
			:	6	6	9	2



		Division	
Skill Year Group	Concrete	Pictorial	Abstract
Solve 1-step problems using multiplication (sharing) Year 1/2	Children are to solve problems by sharing amounts into equal groups. Use physical objects linked to topic, familiar concrete resources etc.	Pictorial representations of the concrete could be used. Bar models also lend themselves well to division problems.	In year 1, there is no expectation at this stage for children to record division formally. In year 2, children are to be introduced to the division symbol and how to represent the calculation in the abstract. $20 \div 5 = 4$
Solve 1-step problems using division (grouping) Year 1/2	Children solve problems by grouping an counting number of groups. This also helps children to see the link between multiplication and division. Use physical objects linked to topic, familiar concrete resources etc.	Grouping encourages children to count in multiples and links to repeated subtraction on a number line.	In year 1, there is no expectation at this stag for children to record division formally. In year 2, children are to be introduced to the division symbol and how to represent the calculation in the abstract. $20 \div 5 = 4$
Divide 2-digits by 1-digit (sharing with no exchange)	When dividing larger numbers, children are to use manipulatives that allow them to partition into tens and ones. Base 10 is a good concrete resource to start with, moving onto place value counters when confident.	Pictorial representations of concrete resources could be used to as a stepping stone between concrete and abstract, but is not necessary.	Part-whole models help to show a clear written method that matches the concrete representations. Children will represent the sum using the division symbol. $48 \div 2 = 24$
Year 3			40 8

		Division	
Skill Year Group	Concrete	Pictorial	Abstract
Divide 2-digits by 1-digit (sharing with exchange)	Children are to use base 10 and/or place value counters when needing to exchange during division.	Pictorial representations of the concrete could be used. Bar models also lend themselves well to division problems.	Flexible partitioning in a part-whole model supports this method and allows children to clearly see the links. The formal written method should be introduced at this stage.
Year 3/4	O 000 O 000 O 000	? ? ? ?	$52 \div 4 = 13$ $\begin{array}{c} 32 \\ 40 \\ 10 \\ 10 \\ 3 \\ 10 + 3 = 13 \end{array}$
Divide 2-digits by 1-digit (sharing with remainders)	Base 10 and/or place value counters should be used when exchanging is taking place. These manipulatives also clearly show the remainders which are left outside of the model after the equal groups have been made.	Pictorial representations of the concrete could be used. Bar models also lend themselves well to division problems.	Flexible partitioning in a part-whole model supports this method and allows children to clearly see the links. The formal written method should be introduced at this stage.
Year 3/4	Tens	13 13 13 1	$53 \div 4 = 13 \text{ r1}$ $\begin{array}{c} 40 & 13 \\ 12 & 1 \\ 10 & 1 \end{array}$
Divide 2-digits by 1-digit (grouping)	Using place value counters and place value grids allow children to group by the divisor clearly starting with the largest place value. Remainders can be seen as the counters left ungrouped.	Pictorial representations of the concrete could be used. Bar models also lend themselves well to division problems.	The formal written method is essential at this stage. Language is important with children considering, for example, "How many groups of 4 tens can we make? And 'How many
Year 4	Tera		groups of 4 ones can be make?' 1 3 4 5 12

		Division	
Skill Year Group	Concrete	Pictorial	Abstract
Divide 3-digits by 1-digit (sharing)	Continue to use place value counters to share into equal groups. This method of grouping equally between the rows (the largest place value first) helps to highlight remainders.	Pictorial representations of the concrete could be used. Bar models also lend themselves well to division problems.	Flexible partitioning in a part-whole model supports this method.
Year 4	Hundreds Tens	? ? ? ?	856
Divide 3-digits by 1-digit (grouping)	Children continue to use grouping to support their understanding of short division. Place value counters or plain counters on a place value grid are the most efficient concrete resources.	Pictorial representations of the concrete could be used. Bar models also lend themselves well to division problems.	At this stage, children should be using the formal written method for division as the abstract form of recording.
Year 5	Hundreds Tens Description of the control of the con		2 1 4 4 8 5 ¹ 6
Divide 4-digits by 1-digit (grouping) Year 5	value grid are the most efficient concrete resources.	Pictorial representations of the concrete could be used. Bar models also lend themselves well to division problems.	Children should be being encouraged to move away from concrete and pictorial representations at this stage and focus on the formal written method.
			2 8 5 13 12

	Division				
Skill Year Group	Concrete	Pictorial	Abstract		
Divide multi-digits by 2 digits (short division) Year 6	Concrete and pictorial become less effective at this stage and children should be encouraged to use the formal written method for division.	Concrete and pictorial become less effective at this stage and children should be encouraged to use the formal written method for division.	Children may choose to write out their multiples to support their calculations, particularly with large remainders being 'carried'. Children should be solving word problems with remainders where the quotient can be rounded as appropriate. O 4 8 9 15 7 7 3 13 13 5 15 15 15 15		
Divide multi-digits by 2 digits (long division) Year 6	Concrete and pictorial become less effective at this stage and children should be encouraged to use the formal written method for division.	Concrete and pictorial become less effective at this stage and children should be encouraged to use the formal written method for division.	Children may choose to write out their multiples to support their calculations, particularly with large remainders being 'carried'. Children should be solving word problems with remainders where the quotient can be rounded as appropriate. $ \begin{array}{c ccccccccccccccccccccccccccccccccccc$		

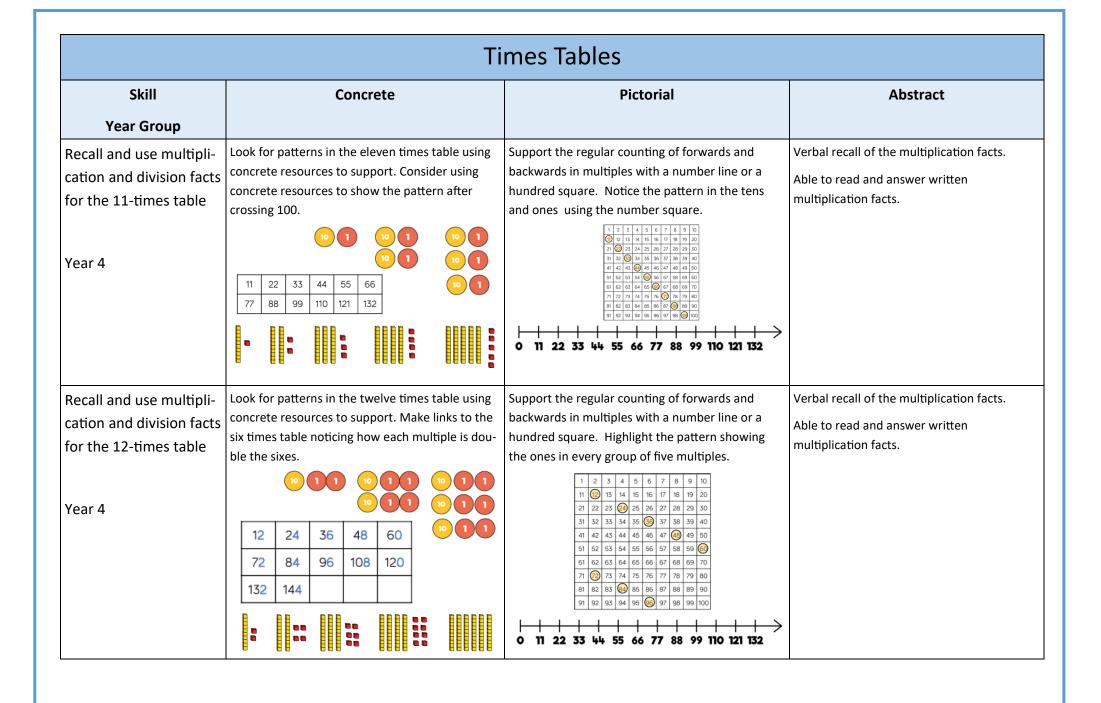


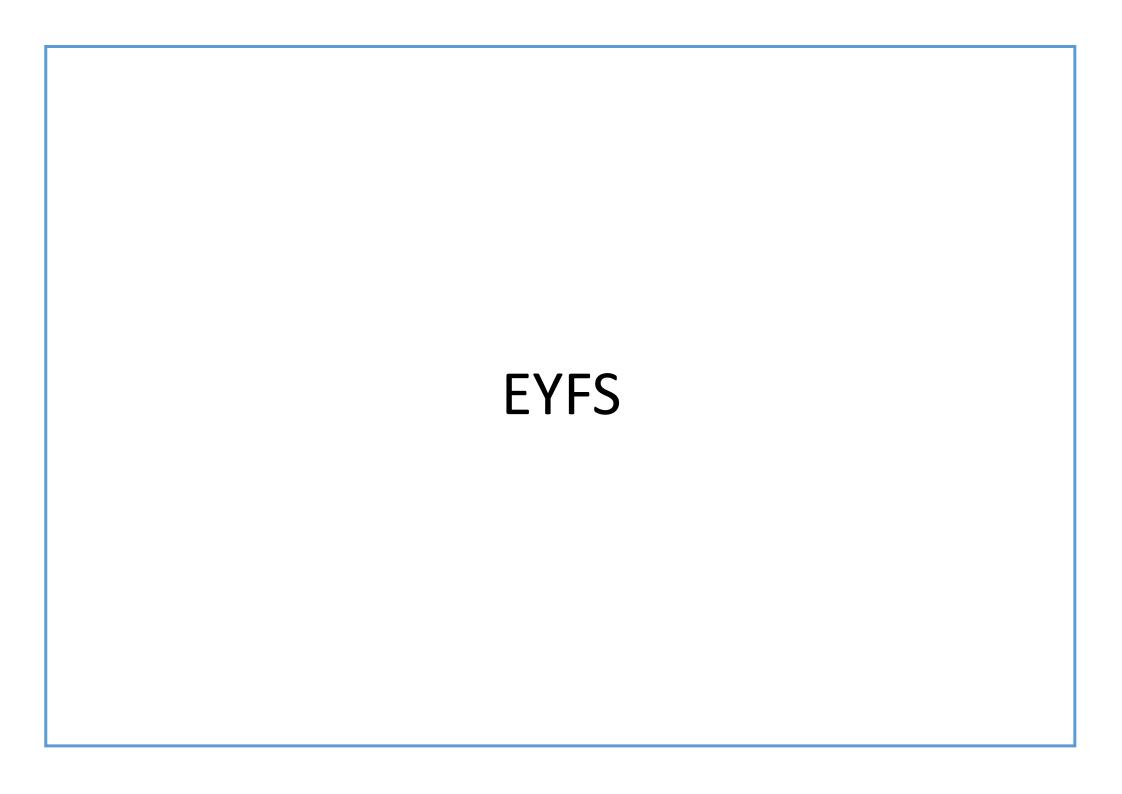
Times Tables			
Skill	Concrete	Pictorial	Abstract
Year Group			
Recall and use multipli-	Look for patterns in the times table using con-	Support the regular counting of forwards and	Verbal recall of the multiplication facts.
cation and division facts	crete resources to support. Notice the pattern in	backwards in multiples with a number line or a	Able to read and answer written
for the 10-times table	the digits—the ones are always zero and the tens increase by 1 each time.	hundred square. 1 2 3 4 5 6 7 8 9 6 11 12 13 14 15 16 17 18 19 6 21 22 23 24 25 26 27 28 29 6 31 32 33 34 35 35 37 38 39 6	multiplication facts.
Year 2		0 10 20 30 40 50 60 70 80 90 100 10 20 30 40 50 60 70 80 90 100 10 20 30 40 50 60 70 80 90 100	
Recall and use multipli-	Look for patterns in the times table using con-	Support the regular counting of forwards and	Verbal recall of the multiplication facts.
cation and division facts	crete resources to support. Notice the pattern in	backwards in multiples with a number line or a	Able to read and answer written
for the 5-times table	the ones as well as highlighting the odd, even, odd, even pattern.	hundred square. 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20	multiplication facts.
Year 2		21 22 23 24 25 26 27 28 29 30 31 32 33 34 35 36 37 38 39 40 41 42 43 44 43 46 47 48 49 30 0 1 2 3 4 5 6 7 8 9 10 11 12 13 14 15 16 17 18 19 20	
Recall and use multipli-	Look for patterns in the times table using con-	Support the regular counting of forwards and	Verbal recall of the multiplication facts.
cation and division facts	crete resources to support. Notice how all of the	backwards in multiples with a number line or a	Able to read and answer written
for the 2-times table	numbers are even and there is a pattern in the ones.	hundred square. 1 ② 3 ④ 5 ⑥ 7 ⑧ 9 ⑩ 11 ⑩ 13 ⑭ 15 ⑯ 17 ⑯ 19 ⑩ 21 ② 23 ② 25 ② 27 ② 29 ⑪ 31 ③ 33 ③ 35 ⑤ 37 ③ 39 ④	multiplication facts.
Year 2		41 43 43 45 47 49 49 GO 0 1 2 3 4 5 6 7 8 9 10 TI 12 13 14 15 16 17 18 19 20	

https://www.ncetm.org.uk/classroom-resources/lv-multiplication/

Times Tables				
Skill	Concrete	Pictorial	Abstract	
Year Group Recall and use multiplication and division facts for the 4-times table Year 3	Look for patterns in the times table using concrete resources to support. Make links to the 2 times table, seeing how each multiple is double the twos. Notice the ones within each group of five multiples. Highlight that all multiples are even using number shapes to support. 4 8 12 16 20 24 28 32 36 40 44 44 48 52 56 60 4 8 12 16	Support the regular counting of forwards and backwards in multiples with a number line or a hundred square. 1 2 3 4 5 6 7 (3) 9 10	Verbal recall of the multiplication facts. Able to read and answer written multiplication facts.	
Recall and use multiplication and division facts for the 8-times table Year 3	Look for patterns in the times table using concrete resources to support. Make links to the 4 times table, seeing how each multiple is double the fours. Highlight that all multiples are even using number shapes to support. 8	Support the regular counting of forwards and backwards in multiples with a number line or a hundred square. 1 2 3 4 5 6 7 (3) 9 10 11 12 13 14 15 (3) 17 18 19 20 21 22 23 (2) 25 26 27 28 29 30 31 (3) 33 34 35 36 37 38 39 (3) 41 42 43 44 45 46 47 (3) 49 50 51 52 53 54 55 (6) 57 58 59 60 61 62 63 (6) 65 66 67 68 69 70 71 (2) 73 74 75 76 77 78 79 (3) 0 8 16 24 32 40 48 56 64 72 80 88 96	Verbal recall of the multiplication facts. Able to read and answer written multiplication facts.	
Recall and use multiplication and division facts for the 3-times table Year 3	Look for patterns in the times table using concrete resources to support. Notice the odd, even, odd, even pattern using number shapes to support.	Support the regular counting of forwards and backwards in multiples with a number line or a hundred square. Highlight the pattern in the ones . 1 2 3 4 5 6 7 8 3 10 10 10 10 10 10 10 10 10 10 10 10 10	Verbal recall of the multiplication facts. Able to read and answer written multiplication facts.	

Times Tables			
Skill	Concrete	Pictorial	Abstract
Year Group			
Recall and use multipli- cation and division facts for the 6-times table	Look for patterns in the six times table using concrete resources to support. Make links to the three times table, seeing how each multiple is double the threes. Highlight that all multiples are	Support the regular counting of forwards and backwards in multiples with a number line or a hundred square. Highlight the pattern in the ones within each group of 5 multiples.	Verbal recall of the multiplication facts. Able to read and answer written multiplication facts.
Year 4	even numbers using shapes to support. 6	1 2 3 4 5 3 7 8 9 10 11 30 13 14 15 16 17 30 19 20 21 22 23 30 25 26 27 28 29 30 31 32 33 34 35 30 35 39 37 38 39 40 41 30 43 44 45 46 47 30 49 50 51 52 53 30 55 56 57 58 59 30 0 6 12 18 24 30 36 42 48 54 60 66 72	
Recall and use multiplication and division facts for the 9-times table	Look for patterns in the nine times table using concrete resources to support. Note the odd, even, odd, even pattern within the multiples.	Support the regular counting of forwards and backwards in multiples with a number line or a hundred square. Notice the pattern in the tens and ones using the number square to support.	Verbal recall of the multiplication facts. Able to read and answer written multiplication facts.
Year 4	9 18 27 36 45 54 63 72 81 90	11 12 15 14 15 16 17 10 10 20 21 22 23 24 25 26 25 26 25 26 25 23 23 24 25 26 25 26 25 26 25 23 23 24 24 24 24 24 24	
Recall and use multiplication and division facts for the 7-times table	There are no obvious patterns within the seven times tables, however, children should be familiar with many of the multiples due to commutativity. Children should be able to still see the odd, even pattern in the multiples.	Support the regular counting of forwards and backwards in multiples with a number line or a hundred square. 1 2 3 4 5 6 2 8 9 10 11 12 13 3 15 16 17 18 19 20 22 23 24 25 26 27 3 29 30 31 32 33 34 36 36 37 38 39 40	Verbal recall of the multiplication facts. Able to read and answer written multiplication facts.
Year 4	7 14 21 28 35 42 49 56 63 70	41 62 43 44 45 46 47 48 69 50 51 52 53 54 55 69 57 58 59 60 61 62 63 64 65 66 67 68 69 70 71 72 73 74 75 76 77 78 79 80 81 82 83 69 85 86 87 88 89 90 90 92 93 94 95 96 97 69 99 100	





Concrete Decople or objects, children add one more oup to find the new total—link to class	Pictorial Children add one more cube/counter/object linked to topic to a group to represent one more. Can we draw what has happened?	Abstract Use number lines to understand how to link counting on with finding one more. O 1 2 3 4 5 6 7 8 9 10 One more than 4 is 5 5 is one more than 4
	linked to topic to a group to represent one more.	counting on with finding one more. O 1 2 3 4 5 6 7 8 9 10 One more than 4 is 5 5 is one more than 4
	One more than 4 is 5	Start to add more than one and understand the link with counting. Could use counters or cubes initially and some may write a number sentence. $4 + 2 = 6$
people or objects, sort them into parts and stand the relationship with the whole.	Draw pictures or diagrams to represent the parts and understand the relationship with the whole. The parts are 3 and 3. The whole is 6.	Use a part-whole model to represent the numbers. Some may progress onto writing a number sentence. $ \begin{array}{cccccccccccccccccccccccccccccccccc$
	s are 3 and 3.	

Addition			
Skill Year Group	Concrete	Pictorial	Abstract
Knowing and finding number bonds within 10	Start with a group, break it apart and put back together again and form number bonds. 4 and 3 makes 7 3 add 4 equals 7 7 = 3 + 4	Use five and tens frames to represent key number bonds. Start with using double sides counters/cubes etc. and move to drawing onto frames. $6+4=10$ $10=4+6$	Use the models from pictorial representation alongside a part-whole model. Show the number bonds. Make sure to include examples where one of the parts is 0.
Adding by counting on	Children to use their knowledge of counting to 20 to find a total by counting on using people or objects. E.g. There's already 8 children on the carpet. Count on as more children sit down.	Use counters or drawings to represent their counting on strategy. 8 on the carpet	

Subtraction			
Skill	Concrete	Pictorial	Abstract
Year Group			
Counting back and taking away	Arrange people or objects and count how many we have. Remove 1 and see how many are left.	Move onto drawing images and crossing out or using counters to represent objects.	Children count back to take away and use a number line or number track to support the method. Some may move onto number sentences.
	1 less that 6 is 5		0 1 2 3 4 5 6 7 8 9 10
	6 subtract 1 is 5	There are animals left.	6 - =
Finding a missing part, given a whole and a part	Separate a whole into two parts and understand how one part can be found by subtracting the other part. 8-5 = ?		
Subtraction within 10	Understand when and how to subtract 1 from a number using an efficient method. Use familiar concrete resources and introduce the concept on a rekenrek. E.g. 5—3 = 2	Representations similar to those used throughout policy e.g. five or ten frames, number lines etc.	Begin to move towards writing number sums which show understanding of number bonds within 10. $5-3=2$
		5—2 = 3	

Division, Doubling and Halving				
Skill	Concrete	Pictorial	Abstract	
Year Group				
Grouping	Learn to make equal groups from a whole and experiment with finding how many equal groups of a certain size can be made. Use people and objects sorting them into areas or hoops etc.	Represent the whole and work out how many equal groups there are using drawings or small objects (e.g. counters) which represent a person or objects.		
	There are 8 children altogether. There are 2 in each group.	There are 10 in total There are 5 in each group.		
	There are 4 groups.	There are 42groups.		
Sharing	Share a set of objects into equal parts and work out how many are in each part.			